

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/42

Paper 4 (Extended) May/June 2016

MARK SCHEME
Maximum Mark: 120

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This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Abbreviations

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

(Question	Answer	Mark	Part Marks
1	(a)	Image at (5, 5), (7, 5), (6, 6), (5, 6)	2	If 0 scored SC1 for translation $\begin{pmatrix} 3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
	(b)	Image at $(-1, -2)$, $(-1, -4)$, $(-2, -3)$, $(-2, -2)$	2	If 0 scored SC1 for reflection in line $y = x$
	(c)	Image at (-2, 5), (-2, 7), (-3, 5), (-3, 6)	3	If 0 scored SC2 for 90° clockwise about (–2, 1) or SC1 for 90° anticlockwise about other centre
	(d) (i)	Enlargement [scale factor] 3 [centre] (2, 4)	B1 B1 B1	If combined transformations, all three marks lost
	(ii)	Stretch [factor] 2 y-axis oe invariant	B1 B1 B1	If combined transformations, all three marks lost
2	(a)	$\frac{630}{9} \times 5$ and $\frac{630}{9} \times 4$ oe	M2	M1 for $630 \div 9$ [=70] or $\frac{5 \times 630 \text{ or } 3150}{9}$ or $\frac{4 \times 630 \text{ or } 2520}{9}$
	(b) (i)	120	3	M2 for 98.4[0] ÷ [0].82 oe or M1 for recognising 98.4[0] is 82%
	(ii)	69.5 or 69.51	3	M2 for $\frac{98.4[0]-30}{98.4[0]} \times 100$ oe or M1 for $\frac{98.4[0]-30}{98.4[0]}$ oe or $\frac{30}{98.4[0]} \times 100$ If 0 scored, SC1 for answer 75%
	(iii)	211.6[0] cao final answer	1	

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Qı	uestion	Answer	Mark	Part Marks
	(iv)	183	4	B3 for answers 182.8 or 182.84 to 182.85 or M2 for $150(1.02)^{10}$ seen oe or M1 for $150(1.02)^n$ seen oe where $n > 1$
	(c)	September or October 2035 nfww	5	B4 for 2035 or 19 years and 9 or 10 or 9.96 or 9.961 to 9.962 months nfww or B3 for 19.8 or 19.83 seen or $\frac{\log\left(\frac{500}{350}\right)}{\log(1.0015)}$ oe or $350 \times 1.0015^n = 500$ and at least two valid trials or sketch of appropriate graph or M1 for $350 \times 1.0015^n = 500$] or $350 \times \left(1 + \frac{0.15}{100}\right)^n = 500$] If 0 scored SC2 for 24[.0] or 23.95 to 23.98 or 2.55 or 2.552 to 2.554 seen
3	(a) (i)	60	1	
	(ii)	8	2	B1 for [lq =] 56 or [uq =] 64
	(iii)	12	2	M1 for 188 seen
	(b)	68.6 or 68.57	3	M2 for $50 \times \frac{2.4}{1.75}$ oe or M1 for <i>their</i> distance $\div 1.75$ or B1 for distance = 120 or for 2.4 and 1.75 or 144 and 105 or 8640 and 6300 seen If 0 scored, SC1 for 77.2 or 77.24
4	(a)	24	3	M2 for $6w + 5(w + 30) = 414$ oe or better or B1 for $6w$ and $5(w + 30)$ oe
	(b)	$2x^2 + 4x - 7 = 0$ oe	B2	i.e. a correct simplified quadratic equation M1 for $x^2 + (x+1)(x+3)$ [=10] oe
		Sketch of appropriate graph or correct use of formula or completing square	M1 dep	Dep on a quadratic from addition of two areas. Must see some valid method
		4.48 or 4.49	B2	B1 for 4.484 to 4.485 or $6\sqrt{2} - 4$ or 1.12 or 1.121 or $1.5\sqrt{2} - 1$

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	Question	Answer	Mark	Part Marks
5	(a)	Any 2 of the following		
		Angle ADX = Angle BCX and same segment oe Angle DAX = Angle CBX and same segment oe Angle AXD = Angle BXC and vertically opp oe	2	B1 for one of the three pairs or for at least two pairs of angles without reasons or with incorrect reasons
	(b)	7.5 oe	2	M1 for $\frac{2}{3} = \frac{5}{BX}$ oe
	(c)	67.2 or 67.20 to 67.21 nfww	3	M2 for [cos =] $\frac{2^2 + 5^2 - 4.61^2}{2 \times 2 \times 5}$
				or M1 for $4.61^2 = 2^2 + 5^2 - 2 \times 2 \times 5\cos(AXD)$
6	(a)	Correct sketch		
			2	M1 for shape i.e. starting at origin then one maximum then one minimum A1 for two zeros to right of $x = 10$ and to the left of $x = 20$
	(b)	13.4 or 13.41 to 13.42 19[.0] or 18.97	1 1	
	(c)	(9.49, 1) or (9.486 to 9.487, 1)	B1 B1	
	(d)	(16.4, -1) or (16.43, -1)	B1 B1	
	(e)	$-1 \leqslant f(x) \leqslant 1$	1	
	(f)	Correct sketch of parabola shape from	B1	
		approximately $y = -1$ 5.48 or 5.477	B1	
7	(a) (i)	576 or 575.8 to 576.0	3	M1 for $\frac{2}{3}\pi \times 5^3$ (262 or 261.7 to 261.8)
				M1 for $\frac{1}{3}\pi \times 5^2 \times 12$ (314 or 314.1 to 314.2)
	(ii)	0.547 or 0.5470 to 0.5472	2FT	FT their (a)(i) M1 for their (a)(i) × 0.95 ÷ 1000
	(iii)	1827 or 1828	2FT	FT with consistent units usual accuracy and truncated M1 for 1000 ÷ their (a)(ii)

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	Question	Answer	Mark	Part Marks
	(iv)	361 or 361.2 to 361.3	4	M1 for $2\pi \times 5^2$ (157 or 157.0 to 157.1) M2 for $\pi \times 5 \times \sqrt{5^2 + 12^2}$ (204 or 204.2) or M1 for $\sqrt{5^2 + 12^2}$ (13)
	(b)	5.37 or 5.369	5	M4 for $\sqrt{\frac{377}{\pi(1+\sqrt{10})}}$ or M3 for $\frac{377}{\pi(1+\sqrt{10})}$ or M2 for $\pi r^2 + \pi r \left(\sqrt{(3r)^2 + r^2}\right) = 377$ or M1 for $r^2 + (3r)^2$ oe
8	(a)	[a, b, c =] -2, 1, 2	1, 1, 1	In any order
		[d=] 0	1	
	(b)	-1	1	
	(c)	-1	1	
	(d)	Parabola vertex downwards and vertex below <i>x</i> -axis	M1	
		Cuts given graph in 5 places	A1	
9	(a)	11	1	
	(b)	$\frac{7}{23}$ oe	1	
	(c)	$\frac{110}{182}$ oe	3	M2 for $\frac{their(a)}{their(a)+3} \times \frac{their(a)-1}{their(a)+2}$ or M1 for a single product of two fractions with first fraction $\frac{their(a)}{their(a)+3}$
	(d)		1	

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Q	uestion	Answer	Mark	Part Marks
10	(a)	31	2	B1 for $[f(7) =]$ 12 or M1 for $2(x^2 - x - 30) + 7$
	(b)	$\frac{x-7}{2}$ oe	2	M1 for $y - 7 = 2x$ or $x = 2y + 7$ or $\frac{y}{2} = x + \frac{7}{2}$
	(c)	(2x+13)(2x+1) final answer	3	B2 for $(2x+7+6)(2x+7-6)$ or for $4x^2 + 28x + 13$ or M1 for $(2x+7)^2 - 36$
	(d)	$\frac{x+5}{x+6}$ final answer nfww	4	B2 for $(x-6)(x+5)$ or SC1 for $(x+a)(x+b)$ where ab = -30 or $a+b = -1$
				and B1 for $(x+6)(x-6)$
11	(a)	5.4[0] or 5.396	2	M1 for $\tan 34 = \frac{AB}{8}$ oe or better
	(b)	20.4 or 20.38 nfww	5	B1 for angle $D = 146$
	(c)	48[.0] or 48.1 or 48.04 to 48.12 cao	2	M2 for $[\sin C =] \frac{8\sin(theirD)}{19}$ or M1 for $\frac{8}{\sin C} = \frac{19}{\sin(theirD)}$ oe A1 for $[\text{angle } C =] 13.6$ or 13.61 to 13.63 OR B1 for angle $A = 56$ M2 for $[\sin C =] \frac{their AB \times \sin(theirA)}{19}$ or M1 for $\frac{their AB}{\sin C} = \frac{19}{\sin(theirA)}$ oe A1 for $[\text{angle } C =] 13.6$ or 13.61 to 13.63 M1 for $0.5 \times their(a) \times 19 \times \sin(90 + their(b))$ oe
12	(a)	n^3 cao	1	
	(b) (i)	392	2	B1 for second differences 14, 20, 26 and 32
	(ii)	$n^3 + n^2$ oe	2	M1 for cubic expression but not n^3 or kn^3 only